

# Chemical Oscillation Frequency Control using Phase-locked Loops

A prototype of biological clocks and their entrainment by light?

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Department of Bioinformatics at School of Biology and Pharmacy  
Modelling Oscillatory Information Processing Group

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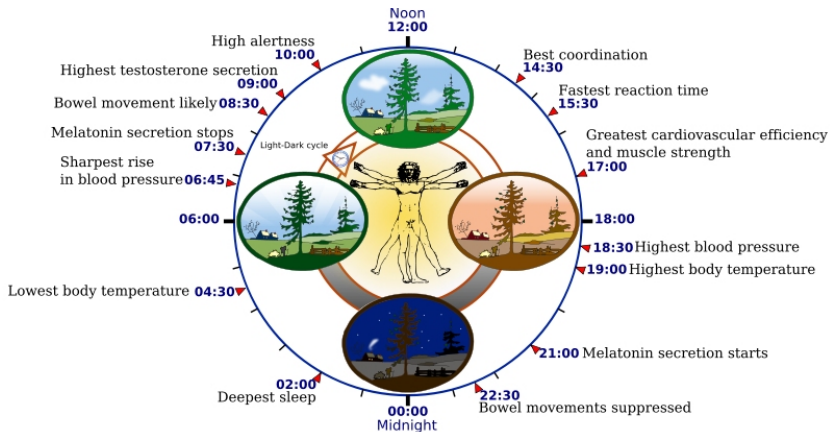
# Systems Biology at Friedrich Schiller University Jena



[www.uni-jena.de](http://www.uni-jena.de)

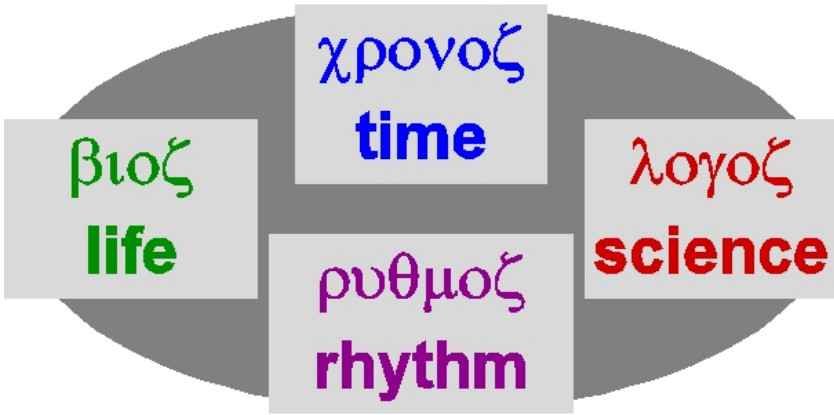


# Human Daily Rhythm: Trigger and Control System



[www.wikipedia.org](http://www.wikipedia.org)

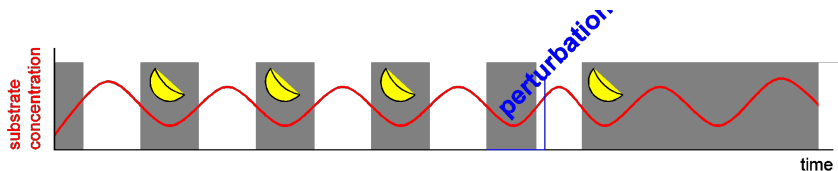
# Chronobiology



science of biological rhythms and clock systems

# Circadian Clock

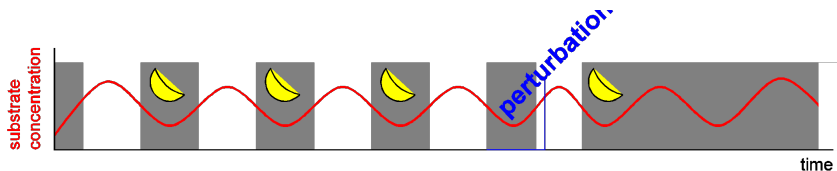
- Undamped biochemical oscillation
- Free-running period close to but typically not exactly 24 hours persisting under constant environmental conditions (e.g. permanent darkness DD or permanent light LL)
- *Entrainment* – adaptation to external stimuli (e.g. light-dark cycles induced by sunlight)
- Temperature compensation within a physiological range
- Reaction systems with at least one feedback loop



⇒ Biological counterpart of frequency control system

# Circadian Clock

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## 1. Reaction Kinetics at a Glance

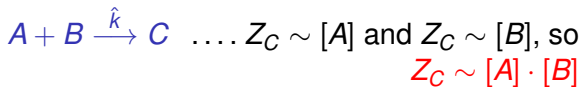
- Mass-action Kinetics: Background
- Ordinary Differential Equations
- Mass-action vs. Saturation Kinetics

2. Processing Units:  
Components of Chemical Control Loops
3. Phase-locked Loop (PLL):  
Continuous Frequency Control
4. Theoretical Background of PLLs
5. Simulation Studies for  
Circadian Clock Systems
6. Prospectives

# Mass-action Kinetics: Background

## Modeling Temporal Behaviour of Chemical Reaction Networks

**Assumption:** number of effective reactant collisions  $Z$  proportional to reactant concentrations (Guldberg 1867)



Production rate generating  $C$ :

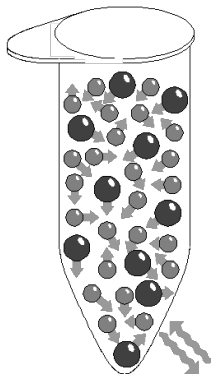
$$v_{prod}([C]) = \hat{k} \cdot [A] \cdot [B]$$

Consumption rate of  $C$ :  $\dots \dots v_{cons}([C]) = 0$

$$\frac{d[C]}{dt} = v_{prod}([C]) - v_{cons}([C])$$

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Initial conditions:  $[C](0), [A](0), [B](0)$   
to be set

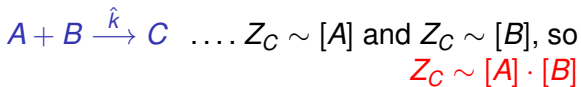




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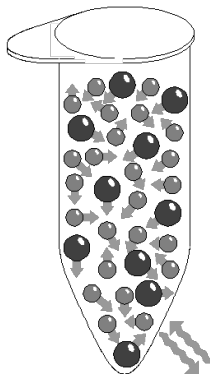
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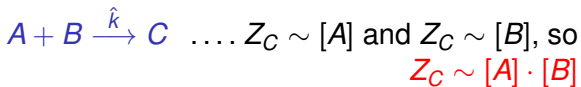
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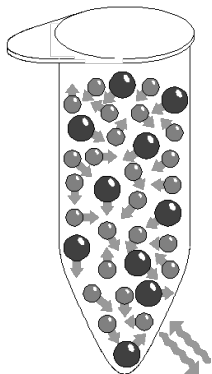
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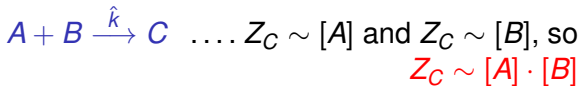
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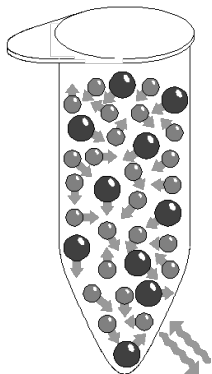
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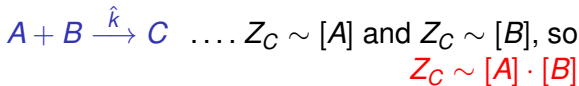
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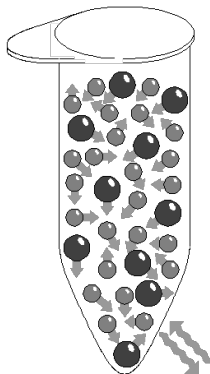
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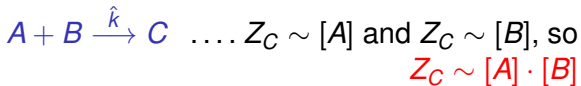
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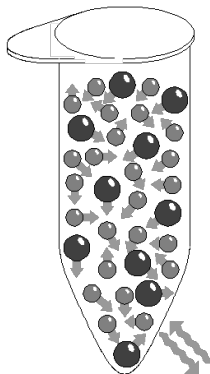
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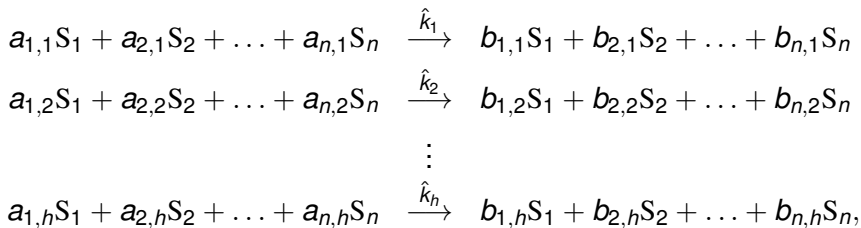
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# Mass-action Kinetics: General ODE Model


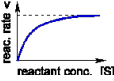
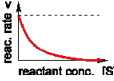
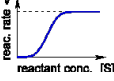
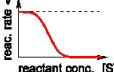
## Chemical reaction system



## results in ordinary differential equations

$$\frac{d[S_i]}{dt} = \sum_{\nu=1}^h \left( \hat{k}_{\nu} \cdot (b_{i,\nu} - a_{i,\nu}) \cdot \prod_{l=1}^n [S_l]^{a_{l,\nu}} \right) \quad \text{with } i = 1, \dots, n.$$

# Mass-action vs. Saturation Kinetics

Kinetics	Activation (rate law)	Repression (rate law)
Mass-action (no saturation)	 $v = k \cdot [S]$	—
Michaelis-Menten (saturation)	 $v = K \cdot \frac{[S]}{T+[S]}$	 $v = K \cdot \left(1 - \frac{[S]}{T+[S]}\right)$
Higher-Order Hill (saturation)	 $v = K \cdot \frac{[S]^n}{T+[S]^n}$	 $v = K \cdot \left(1 - \frac{[S]^n}{T+[S]^n}\right)$

- Michaelis Menten: Typical enzyme kinetics
- Higher-order Hill ( $n \geq 2$ ): Typically for gene expression using sigmoidal transfer function

## 1. Reaction Kinetics at a Glance

## 2. Processing Units: Components of Chemical Control Loops

- Addition
- Multiplication
- Low-pass Filter
- Controllable Goodwin-type Core Oscillator

## 3. Phase-locked Loop (PLL): Continuous Frequency Control

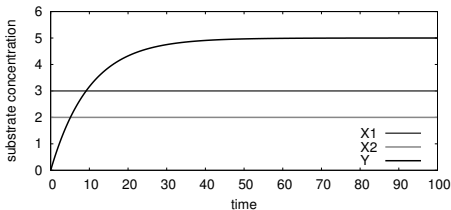
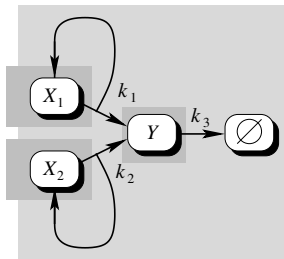
## 4. Simulation Studies for Circadian Clock Systems

## 5. Theoretical Background of PLLs

## 6. Prospectives



# Addition



$$\begin{aligned} \dot{[X_1]} &= 0 \\ \dot{[X_2]} &= 0 \\ \dot{[Y]} &= k_1[X_1] + k_2[X_2] - k_3[Y] \end{aligned}$$

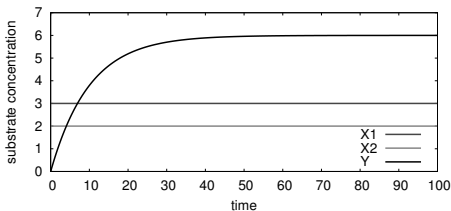
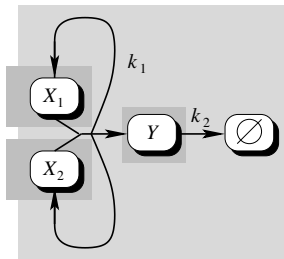
**ODE solution for asymptotic steady state in case of  $k_1 = k_2 = k_3$ :**

$$[Y](\infty) = \lim_{t \rightarrow \infty} (1 - e^{-k_1 t}) \cdot ([X_1](t) + [X_2](t)) = [X_1](0) + [X_2](0)$$

**Transfer function:**  $[Y] = [X_1] + [X_2]$

T. Hinze, C. Bodenstein, B. Schau, I. Heiland, S. Schuster. Chemical Analog Computers for Clock Frequency Control Based on P Modules. Proceedings of the Twelfth International Conference on Membrane Computing, to appear within series Lecture Notes in Computer Science, Springer Verlag, 2011, accepted

# Multiplication



$$\begin{aligned} \dot{[X_1]} &= 0 \\ \dot{[X_2]} &= 0 \\ \dot{[Y]} &= k_1[X_1][X_2] - k_2[Y] \end{aligned}$$

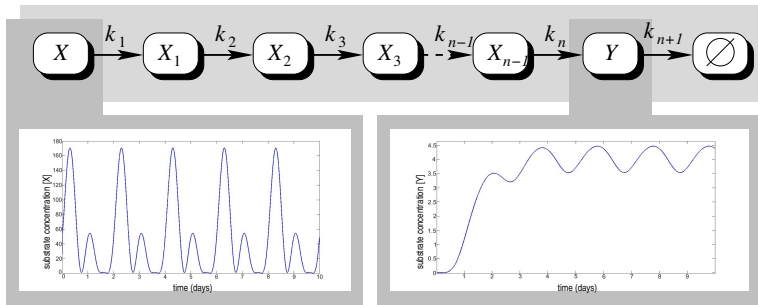
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# Low-pass Filter



$$\dot{[X_1]} = k_1[X] - k_2[X_1]$$

$$\dot{[X_2]} = k_2[X_1] - k_3[X_2]$$

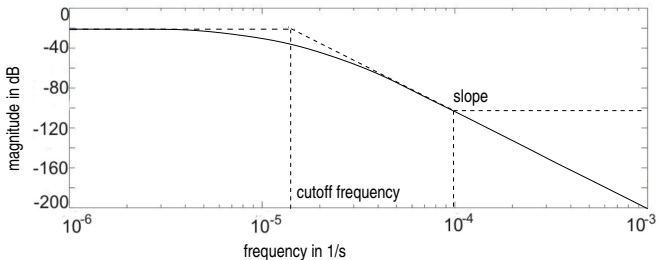
$$\vdots$$

$$\dot{[X_{n-1}]} = k_{n-1}[X_{n-2}] - k_n[X_{n-1}]$$

$$\dot{[Y]} = k_n[X_{n-1}] - k_{n+1}[Y]$$

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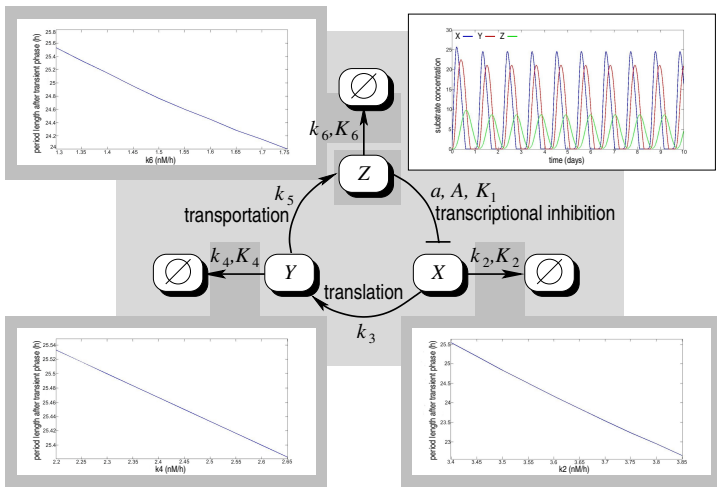
# Low-pass Filter: Bode Plot as Characteristic Curve



$$\text{Magnitude dB} = 10 \cdot \lg \left( \frac{\text{amplitude of output signal}}{\text{amplitude of input signal}} \right)$$

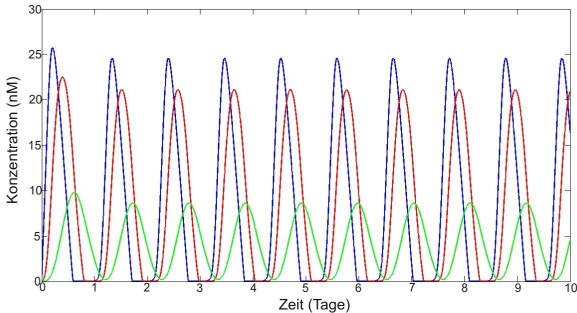
- Signals affected by smoothing delay throughout cascade
- Oscillation waveform harmonisation into sinusoidal shape
- Global filter parameters:  
passband damping, cutoff frequency, slope

# Controllable Goodwin-type Core Oscillator



T. Hinze, C. Bodenstein, B. Schau, I. Heiland, S. Schuster. Chemical Analog Computers for Clock Frequency Control Based on P Modules. Proceedings of the Twelfth International Conference on Membrane Computing, to appear within series Lecture Notes in Computer Science, Springer Verlag, 2011, accepted

# Core Oscillator: Dynamical Behaviour



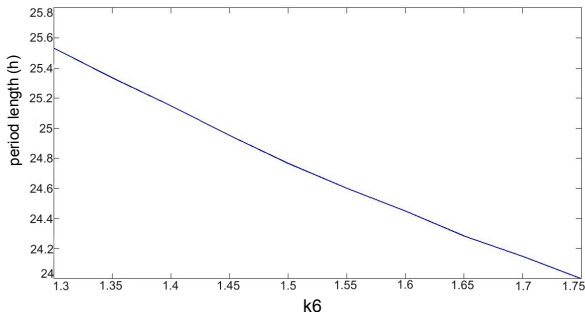
$$\dot{[X]} = \frac{a}{A + K_1[Z]^2} - \frac{k_2[X]}{K_2 + [X]}$$

$$\dot{[Y]} = k_3[X] - k_5[Y] - \frac{k_4[Y]}{K_4 + [Y]}$$

$$\dot{[Z]} = k_5[Y] - \frac{k_6[Z]}{K_6 + [Z]}$$

B. Schau. Reverse-Engineering circadianer Oszillationssysteme als Frequenzregelkreise mit Nachlaufsynchronisation. Diploma thesis, 2011

# Core Oscillator: Dynamical Behaviour



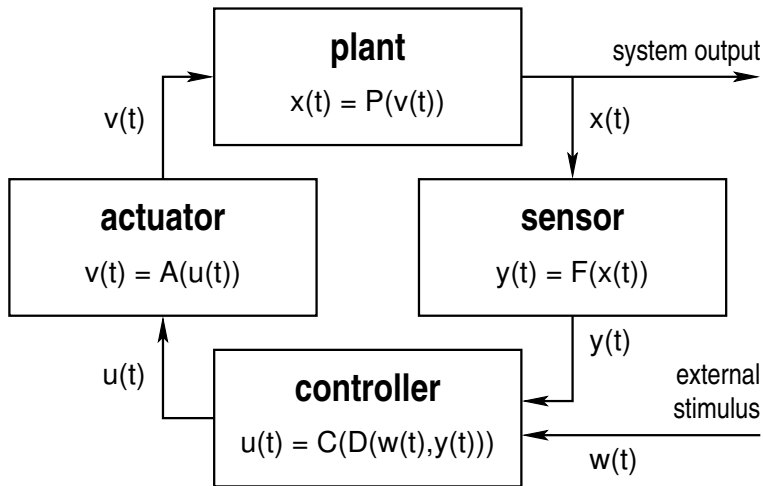
- Velocity parameter  $k_6$  of  $Z$  degradation notably influences oscillation frequency
- Period control coefficients assigned to each reaction quantify influence on frequency

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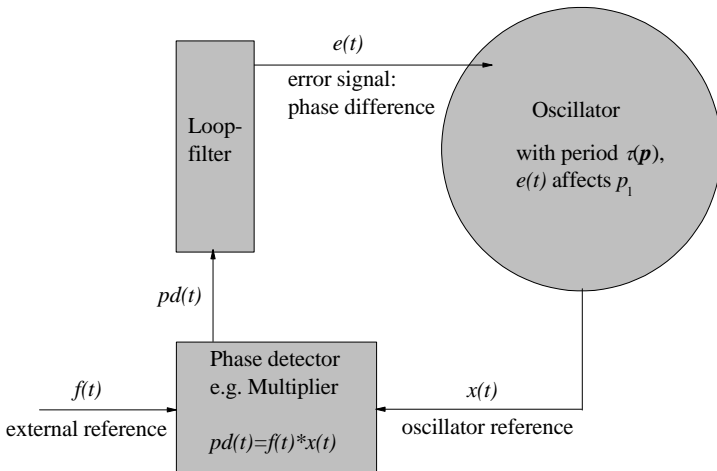
1. Reaction Kinetics at a Glance
2. Processing Units:  
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3. **Phase-locked Loop (PLL):  
Continuous Frequency Control**
  - General Scheme of a Simple Control Loop
  - Scheme of a Phase-locked Loop
  - Model of a Chemical Frequency Control Based on PLL
4. Theoretical Background of PLLs
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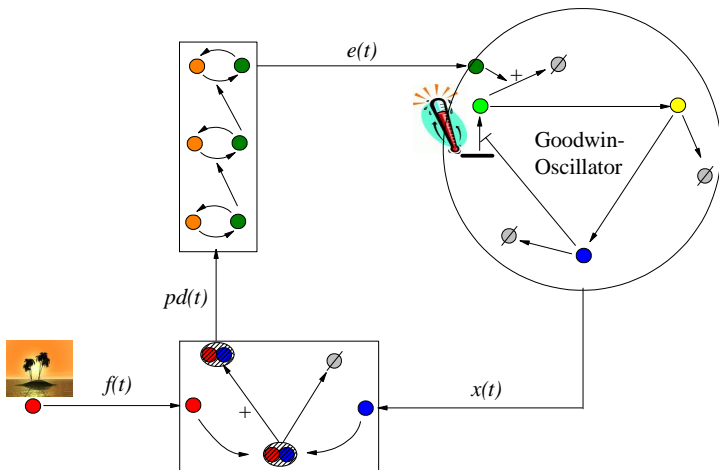
# General Scheme of a Simple Control Loop



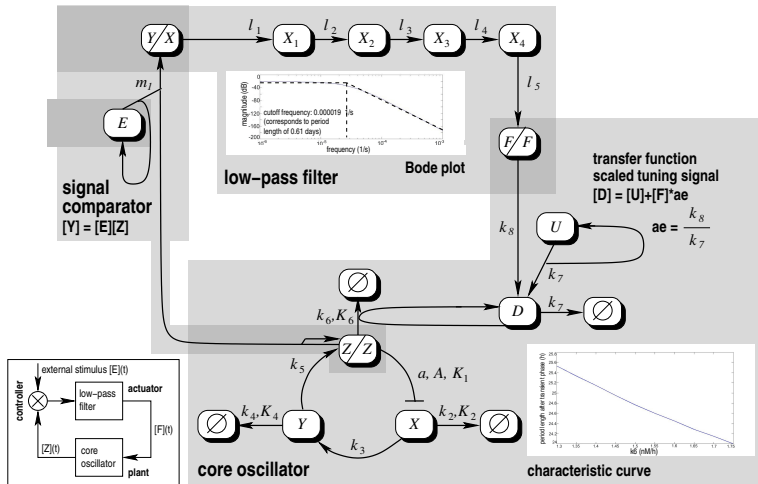
# Scheme of a Phase-locked Loop



# Scheme of a Phase-locked Loop



# Model of a Chemical Frequency Control Based on PLL



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4. **Theoretical Background of PLLs**
  - Comparing Phases
  - Extracting Phase-difference Information
  - Phase Response Curve
  - Amplitude and Phase: Arnold Tongue
5. Simulation Studies for  
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## Comparing Phases

Output of core oscillator  $\omega = 2\pi/\tau$ :

$$y(t) = y(t + \tau) = A_0 + \sum_{n=1}^{\infty} A_n \cos(n\omega t + \varphi_n)$$

Input of external reference signal  $\omega' = 2\pi/\tau'$ :

$$z(t) = z(t + \tau') = A'_0 + \sum_{n=1}^{\infty} A'_n \sin(n\omega' t + \varphi'_n)$$

For simplicity we assume that all higher harmonics are removed by a filter.

# Comparing Phases: Multiplication

Multiplication module:

$$\dot{x} = k(z(t)y(t) - x) \quad \lim_{k \rightarrow \infty} x(t) = z(t)y(t)$$

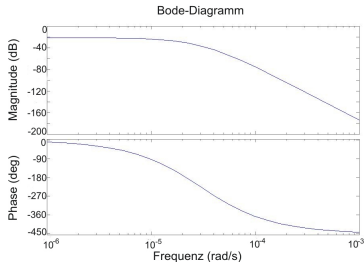
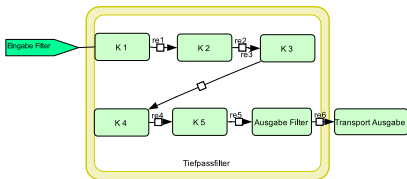
Output of multiplication:

$$z(t)y(t) = A'_0 A_0 + A'_0 A_1 \cos(\omega t + \varphi_1) + A_0 A'_1 \sin(\omega' t + \varphi'_1) \\ + \frac{A'_1 A_1}{2} (\sin((\omega' - \omega)t + \varphi'_1 - \varphi_1) + \sin((\omega' + \omega)t + \varphi'_1 + \varphi_1))$$

Low frequency term ( $\omega' \approx \omega$ ) carries the phase-difference information:  $\phi' - \phi$ .

# Extract Phase-difference Information: Filtering

Filter out high-frequency terms from  $x(t)$ . Simple linear signalling cascade works as a low-pass filter<sup>1</sup>:



B. Schau. Reverse-Engineering circadianer Oszillationssysteme als Frequenzregelkreise mit Nachlaufsynchronisation. Diploma thesis, 2011

Adjust kinetic parameters to obtain desired filtering.

<sup>1</sup>Samoilov et al. *J Phys Chem* 106 (2002)



## Error Signal and Feedback

Output of cascade:

$$e(t) = a_0 + a_1 \sin((\omega' - \omega)t + \varphi'_1 - \varphi_1 + \varphi_{lpf})$$

Weakly (!) feed back the signal to the oscillator, e.g. by changing the kinetic rate constant of  $l$ -th reaction:

$$\begin{aligned} k_1^* &= k_1(1 + \varepsilon e(t)) = k_1 + k_1 \varepsilon a_0 + k_1 \varepsilon a_1 \sin(\dots) \\ &= \tilde{k}_1 (1 + \tilde{\varepsilon} \sin(\dots)). \end{aligned}$$

$\tilde{k}_1$  reaction rate at constant external signal  $A'_0$ . Drop tilde for convenience.

## Perturbed Core Oscillator

Unperturbed core oscillator at constant external signal  $A'_0$ :

$$\frac{d\mathbf{X}}{dt} = \mathbf{F}(\mathbf{X})$$

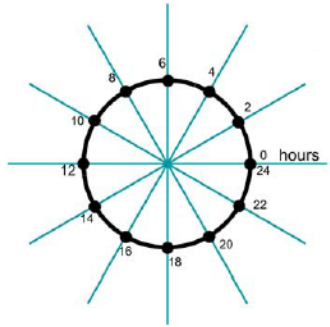
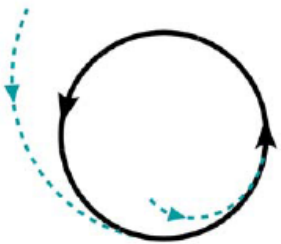
with limit cycle solution  $\mathbf{X}^0(t) = \mathbf{X}^0(t + \tau)$ .

Perturbed core oscillator:

$$\frac{d\mathbf{X}}{dt} = \mathbf{F}(\mathbf{X}) + \varepsilon \sin(\dots) k_1 \frac{\partial \mathbf{F}}{\partial k_1}(\mathbf{X}).$$

Since  $\varepsilon$  is small the amplitude of the limit cycle is not affected and we can reduce the model to the phase dynamics!

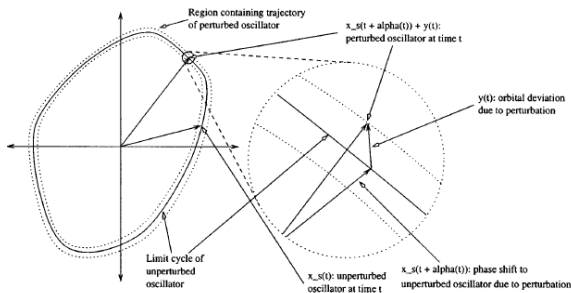
# Amplitude and Phase



Granada & Herzel *PLoS ONE* 4(9): e7057 (2009)

We can assign each point on the limit cycle  $\mathbf{X}^0$  a specific phase value  $\phi$ .

# Phase Reduction (Kuramoto 1984)



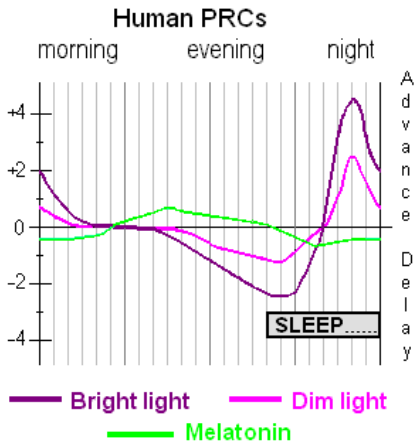
Demir et al. *IEEE Transactions on circuits and systems* 47:5 (2000) 655-674

## Oscillator phase dynamics:

$$\frac{d\phi}{dt} = \omega + \varepsilon \text{PRC}_I(\phi) \sin(\phi' - \phi + \varphi_{Ipf}) .$$

$\text{PRC}_I$  is the  $2\pi$ -periodic phase response curve of  $k_I$ .

# Phase Response Curve



[http://en.wikipedia.org/wiki/Phase\\_response\\_curve](http://en.wikipedia.org/wiki/Phase_response_curve)

## Phase Difference

Phase difference  $\psi$  between oscillator and external signal:

$$\psi = \phi - \phi'$$
$$\frac{d\psi}{dt} = \omega - \omega' - \varepsilon \text{PRC}_I(\phi' + \psi) \sin(\psi - \varphi_{Ipf})$$

$\psi$  is a slowly changing variable compared to  $\phi' = \omega' t$ , therefore we may average the perturbation over one external cycle and consider  $\psi$  on the slow time scale:

$$\frac{1}{\tau'} \int_0^{\tau'} \text{PRC}_I(\phi'(t) + \psi) dt = -C_1^\tau,$$

where  $C_1^\tau = k_1/\tau \frac{\partial \tau}{\partial k_1}$  is the period control coefficient.

# Phase Difference

Phase difference equation:

$$\frac{d\psi}{dt} = \frac{\omega - \omega'}{\varepsilon} + C_1^T \sin(\psi - \varphi_{lpf})$$

Phase-locking corresponds to (stable) steady-state solutions  $\psi_0$  of this equation:

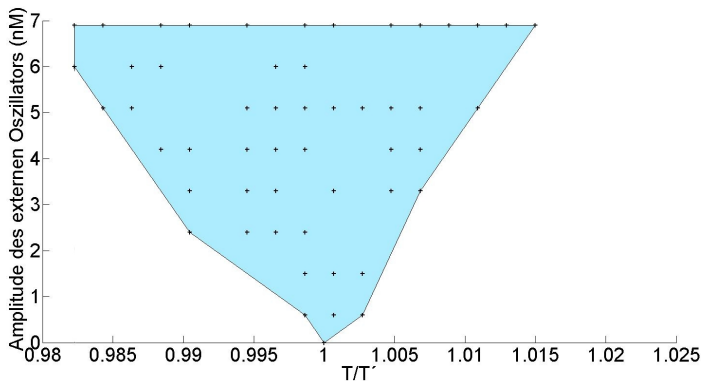
$$\phi(t) = \phi'(t) + \psi_0.$$

Phase locking exists in a region enclosed by:

$$\varepsilon^{\pm} = \mp (\omega - \omega') \frac{1}{C_1^T},$$

the so called *Arnold* tongue.

# Arnold Tongue



B. Schau. Reverse-Engineering circadianer Oszillationssysteme als Frequenzregelkreise mit Nachlaufsynchronisation. Diploma thesis, 2011



# Phase Lag

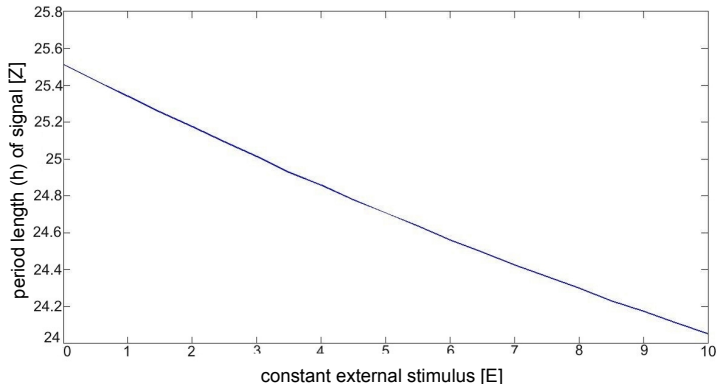
The phase lag can be easily determined from the derived equation. For example consider  $\omega = \omega'$  and  $C_1^T < 0$ , the stable solution then is:

$$\psi_0 = \varphi_{lpf}.$$

That means the phase lag is completely determined by the low-pass filter.

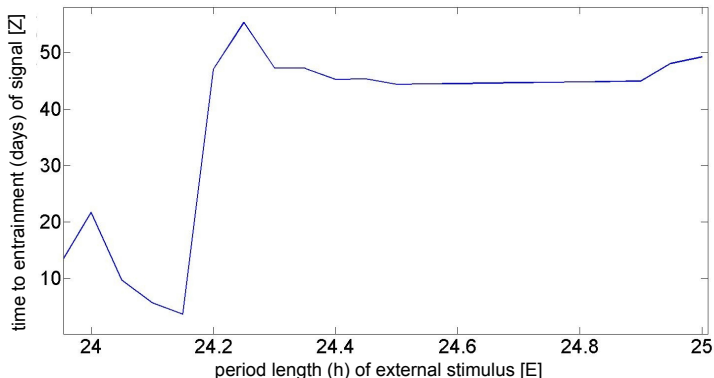
1. Reaction Kinetics at a Glance
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Components of Chemical Control Loops
3. Phase-locked Loop (PLL):  
Continuous Frequency Control
4. Theoretical Background of PLLs
5. **Simulation Studies for Circadian Clock Systems**
  - Period Lengths subject to Constant Ext. Stimulus
  - Time to Entrainment to Different Period Lengths
  - Time to Entrainment to Different Initial Phase Shift
  - Best Case and Worst Case Entrainment
6. Prospectives

# Period Lengths subject to Constant External Stimulus



T. Hinze, C. Bodenstein, B. Schau, I. Heiland, S. Schuster. Chemical Analog Computers for Clock Frequency Control Based on P Modules. Proceedings of the Twelfth International Conference on Membrane Computing, to appear within series Lecture Notes in Computer Science, Springer Verlag, 2011, accepted

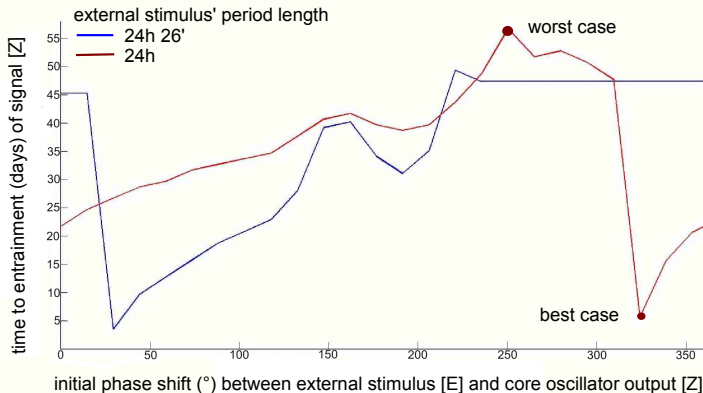
# Time to Entrainment to Different Period Lengths



## Natural period of core oscillator: 24.2h

T. Hinze, C. Bodenstein, B. Schau, I. Heiland, S. Schuster. Chemical Analog Computers for Clock Frequency Control Based on P Modules. Proceedings of the Twelfth International Conference on Membrane Computing, to appear within series Lecture Notes in Computer Science, Springer Verlag, 2011, accepted

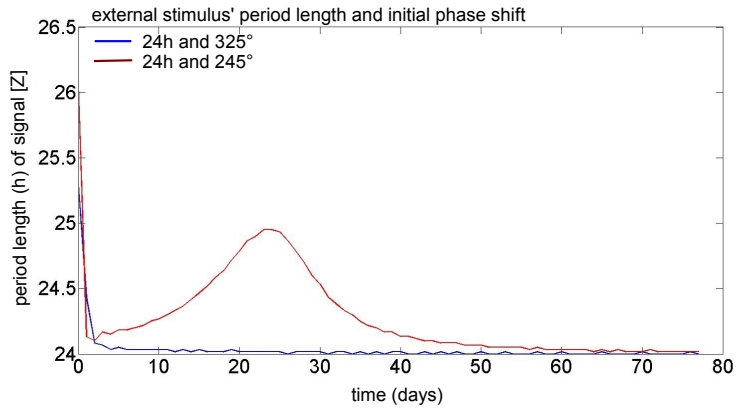
# Time to Entrainment to Different Initial Phase Shifts



## Entrainment reached within convergence interval 1 min

T. Hinze, C. Bodenstein, B. Schau, I. Heiland, S. Schuster. Chemical Analog Computers for Clock Frequency Control Based on P Modules. Proceedings of the Twelfth International Conference on Membrane Computing, to appear within series Lecture Notes in Computer Science, Springer Verlag, 2011, accepted

# Best Case and Worst Case Entrainment



Entrainment reached within convergence interval 1 min

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  - Conclusions and Open Questions
  - Acknowledgements

# Conclusions

- **Chemical frequency control can utilise PLL**
- Prototypic modelling example for entrainment of circadian clockworks
- Chemical processing units in minimalistic manner
- Variety of chemical implementations
- Modularisation in (bio)chemical reaction systems

## Some open questions

- Identification of *in-vivo* counterparts
- Replacement of individual processing units (like different core oscillators)
- Balancing advantages and limitations of the PLL approach
- Inclusion of temperature entrainment (by Arrhenius terms)
- Alternative concepts of frequency control



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# Acknowledgements



Department of Bioinformatics at School of Biology and Pharmacy  
Friedrich Schiller University Jena



Jena Centre for  
Bioinformatics



Research Initiative in  
Systems Biology



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